

Roll.No.

20UCHAT1001

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai - 600 044.

B.Sc.Chemistry- END SEMESTER EXAMINATIONS - NOVEMBER 2025
SEMESTER - I

20UCHAT1001 - Allied Mathematics - I

Total Duration : 2 Hrs.30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Show that $\frac{1}{2}(e - \frac{1}{2}) = 1 + \frac{1}{3!} + \frac{1}{5!} + \dots$
2. Express $\cos 6\theta$ as a polynomial in $\cos \theta$.
3. Apply Newton's backward difference formula to compute a polynomial of degree 3, using the table given below.

x	3	4	5	6
y	6	24	60	120

4. If $\tan^{-1}(2 - i) = x + iy$, show that $4y = -\log 2$.
5. If $A = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$ then show that A is orthogonal.
6. If $\frac{\sin\theta}{\theta} = \frac{2165}{2166'}$ Examine that θ is equal to $3^\circ 1'$ nearly.
7. Given the following values for x and y

x	0	1	2	3	4	5
y	3	12	81	200	100	8

Find $\Delta^5 y_0$

8. If $\sin(A + iB) = x + iy$, then prove that $x = \sin A \cos h B$.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Find the Sum the series $1 + \frac{1}{3} + \frac{1}{3} \cdot \frac{3}{6} + \frac{1}{3} \cdot \frac{3}{6} \cdot \frac{5}{9} + \dots$

10. Compute the Eigenvalue and Eigenvectors of

$$\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$

contd.....

11. Prove that $-2^{10} \cos^5 \theta \sin^6 \theta = \cos 11\theta - \cos 9\theta - 5 \cos 7\theta + 5 \cos 5\theta + 10 \cos 3\theta - 10 \cos \theta$.

12. Use Lagrange's formula to compute y when $x=2$, given

x	0	3	5	6	8
y	276	460	414	343	110

13. If $\tan(\theta + i\varphi) = \cos \alpha + i \sin \alpha$, then prove that

i) $\tan h 2\varphi = \sin \alpha$.

ii) $\cos h 2\varphi = \sec \varphi$.
